

# Simulating a Vibrating Cantilever with COMSOL

Trey Cole

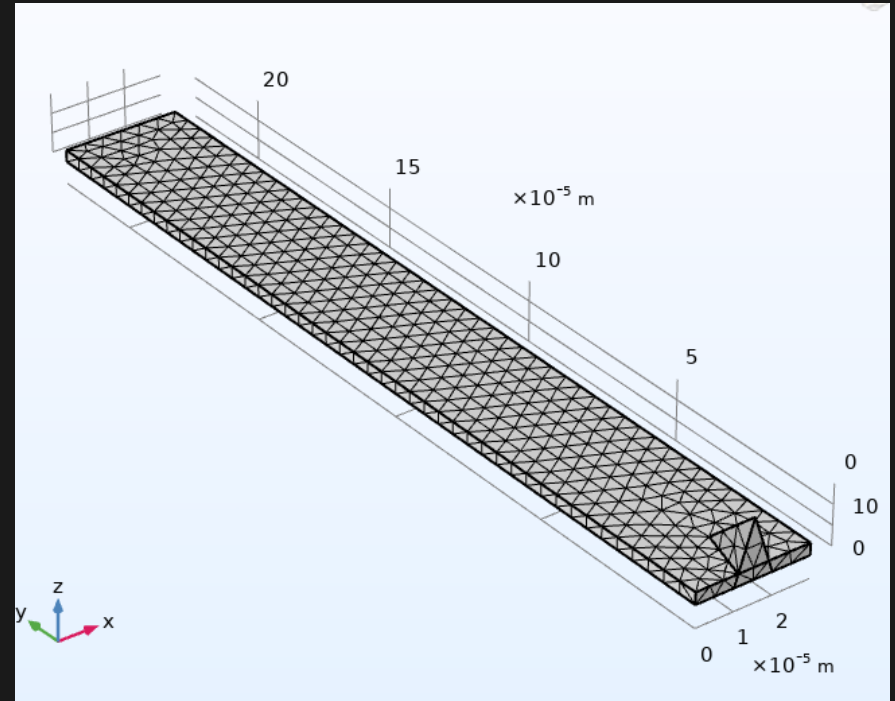
Advisor: Joseph Kopanski

Host: NIST

The logo for the National Institute of Standards and Technology (NIST), consisting of the letters "NIST" in a bold, black, sans-serif font.The logo for the American Institute of Physics (AIP), featuring the letters "AIP" in a large blue font above a yellow horizontal line, with the text "American Institute of Physics" in a smaller blue font below the line.

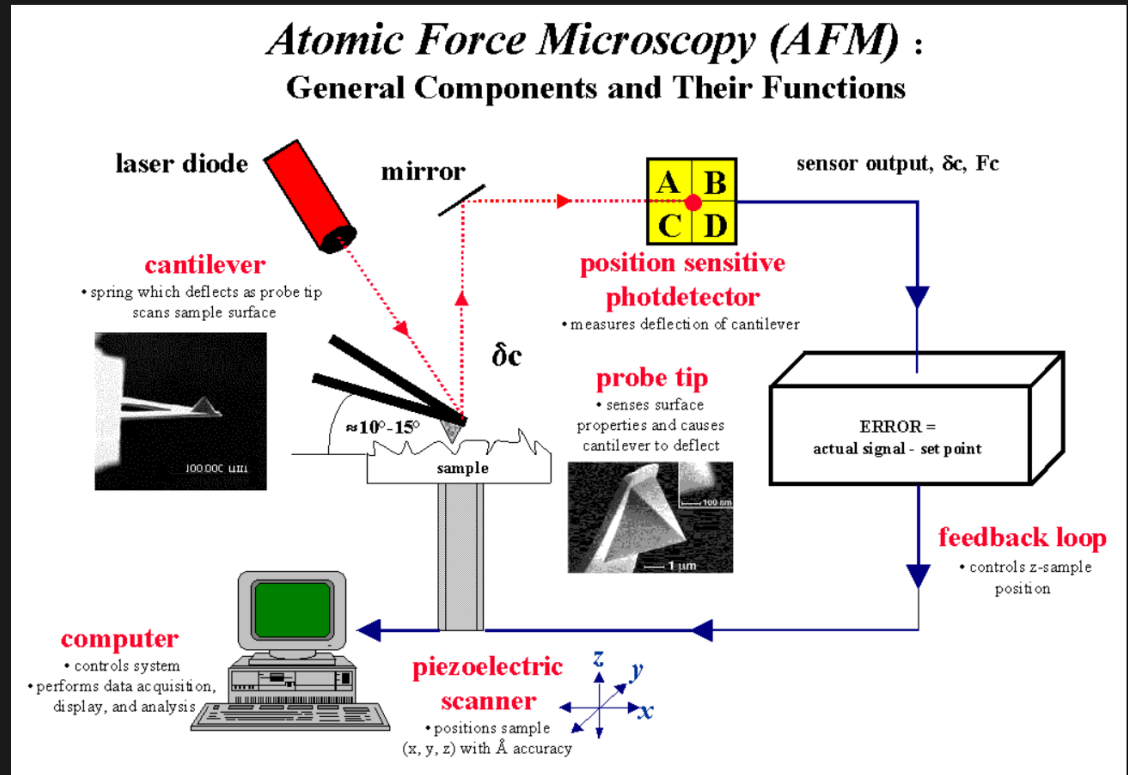
# COMSOL Simulations

- COMSOL is a powerful physics simulation software
- Uses finite element analysis to solve PDE's numerically
  - Quantum Mechanics (Schrodinger's Equation)
  - Electricity and Magnetism (Poisson/Laplace's Equations)
  - Thermodynamics (Heat Equation)
  - Mechanical Systems (Stress and Strain)



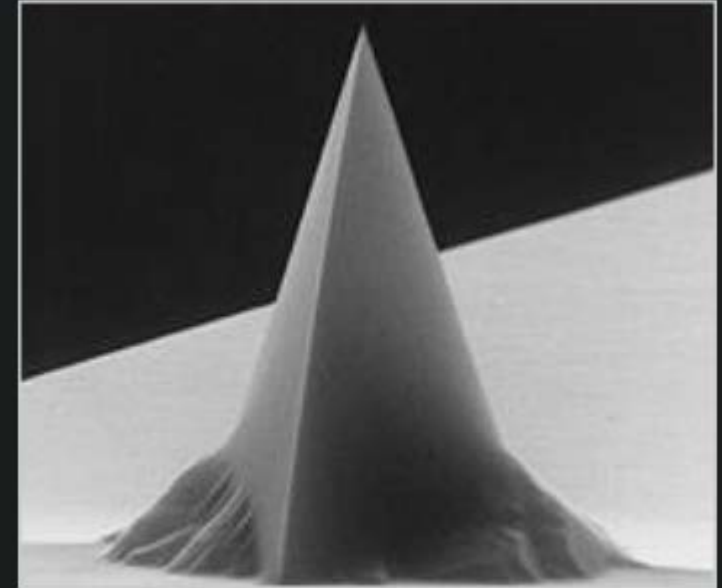
# Atomic Force Microscopy

- Images material's surface
- Images surface details with sub-nanometer resolution ~ 1000+ times better than optical
- Measures Van der Waals atomic forces



# Operational Modes of AFM

- **Contact AFM**
  - Interaction forces are mostly repulsive in this regime due to electron repulsion
- **Non-contact AFM**
  - Tip hovers 10-150 [Å] above sample, scanned across.
  - Offers the advantage of measuring sensitive (soft) materials
- **Tapping AFM**
  - Combines both so that sensitive materials are protected and resolution is better

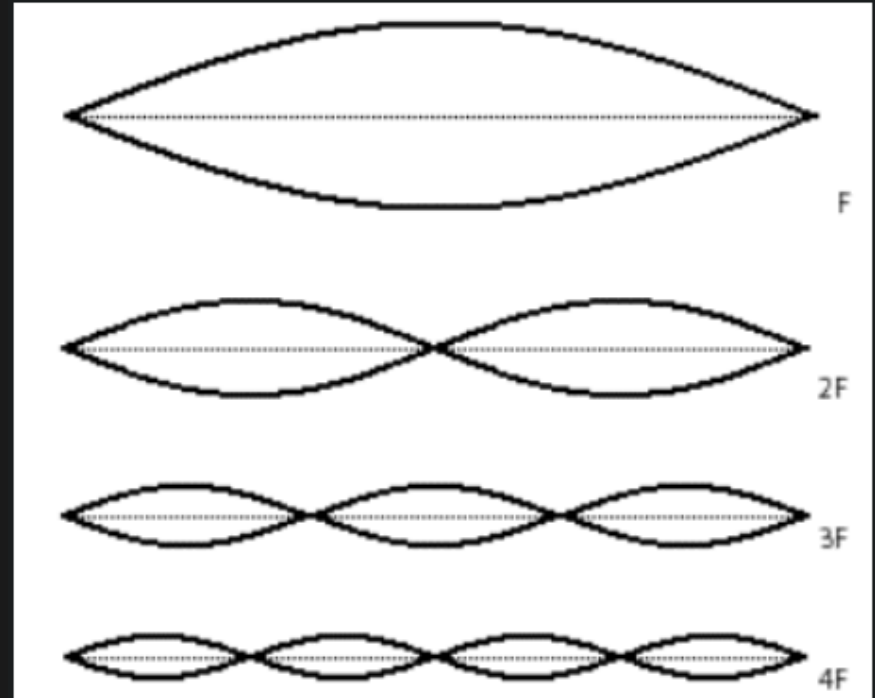


Point Probe AFM tip

<https://www.nanoworld.com/pointprobe-electrostatic-force-microscopy-afm-tip-efm>

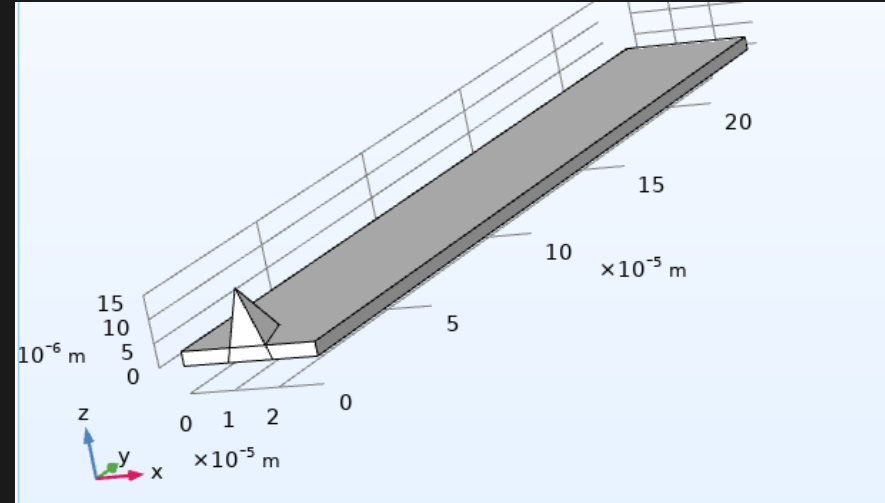
# Resonance and Eigenmodes of Cantilever

- Resonance of the cantilever-tip system is an important aspect of non-contact and tapping mode AFM.
- Thus, it is useful to see the modes of oscillations, and their corresponding frequency for a given material and geometry



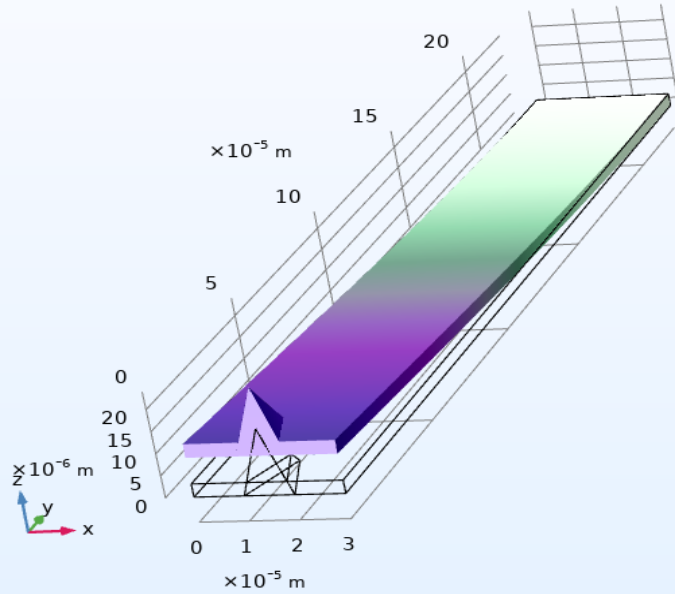
# Cantilever in COMSOL

- Cantilever geometry is  $30\ \mu\text{m}$  in width,  $225\ \mu\text{m}$  in length and  $3\ \mu\text{m}$  in thickness
- The material is p-type Silicon with a Platinum undercoating
- A point load of  $0.6\ \text{nN}$  is applied to the tip of the cantilever

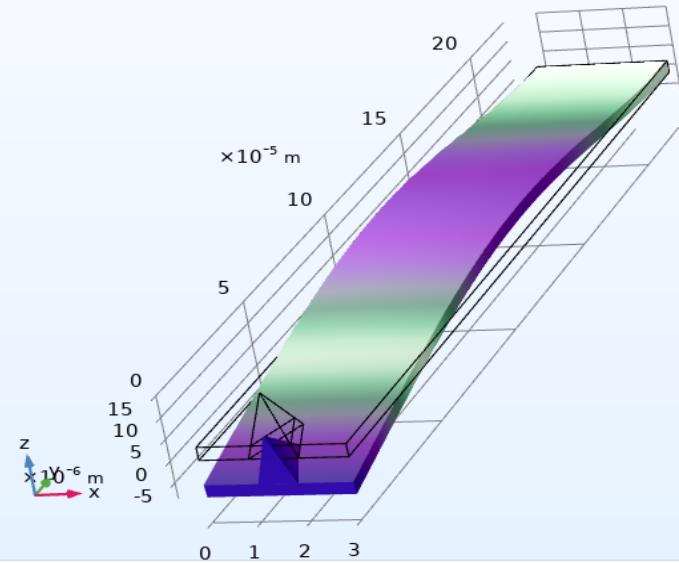


# Vibrational Modes

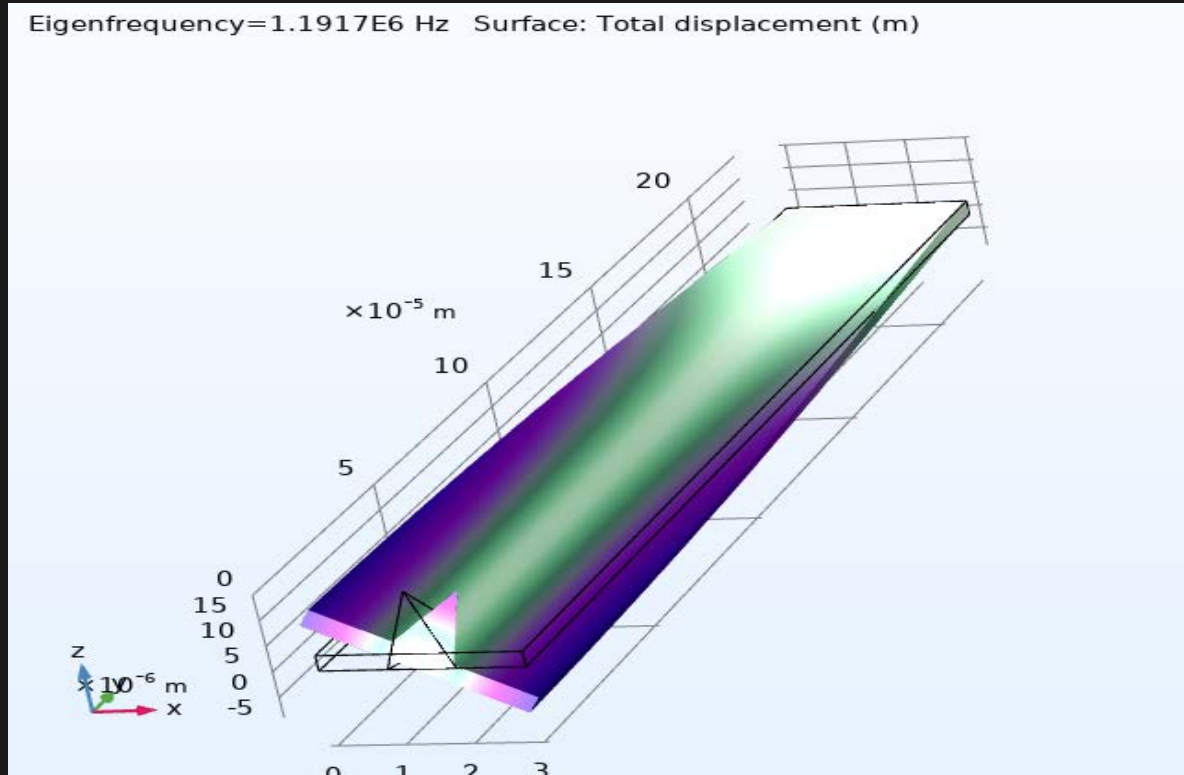
Eigenfrequency=80795 Hz Surface: Total displacement (m)



Eigenfrequency=5.0718E5 Hz Surface: Total displacement (m)



# Torsional Mode





# Acknowledgments

Special thanks to

- My mentor Joseph Kopanski
- The SPS internship staff